

$$\sin \frac{u}{2} = \pm \sqrt{\frac{1 - \cos u}{2}}$$

$$\frac{\pi}{2} < u < \frac{\pi}{2}$$

$$\sin \frac{u}{2} = \sqrt{\frac{1 - \frac{-\sqrt{5}}{3}}{2}}$$

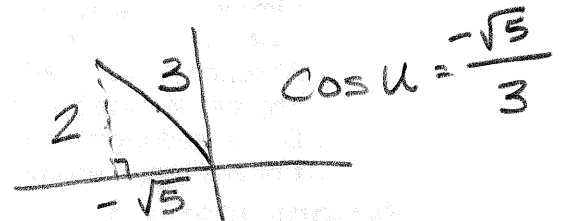
$$\frac{\pi}{4} < \frac{u}{2} < \frac{\pi}{2}$$

Quad I

$$= \sqrt{\frac{1 + \frac{\sqrt{5}}{3}}{2}}$$

$$\sin u = \frac{2}{3} \text{ in Quad II}$$

$$= \sqrt{\frac{\frac{3 + \sqrt{5}}{3} \cdot \frac{1}{2}}{2 \cdot \frac{1}{2}}}$$



$$a^2 + 2^2 = 3^2$$

$$a^2 + 4 = 9$$

$$a^2 = 5$$

$$a = \sqrt{5}$$

$$= \sqrt{\frac{3 + \sqrt{5}}{6}}$$

$$= \frac{\sqrt{3 + \sqrt{5}} \cdot \sqrt{6}}{\sqrt{6} \cdot \sqrt{6}}$$

$$= \frac{\sqrt{3 \cdot 6 + 6\sqrt{5}}}{\sqrt{36}}$$

$$= \frac{\sqrt{18 + 6\sqrt{5}}}{6}$$

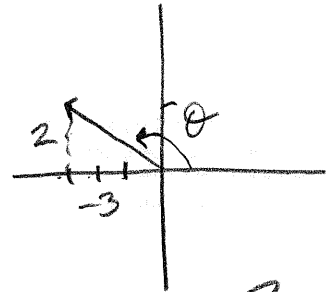
#19 $\vec{A} = \langle -3, 2 \rangle$ and $\vec{B} = \langle 1, 4 \rangle$

a. $\|\vec{A}\|$ and θ

$$\|\vec{A}\|^2 = (-3)^2 + (2)^2$$

$$\|\vec{A}\| = \sqrt{9+4}$$

a) Magnitude = $\sqrt{13}$
angle $\theta = 146.31^\circ$



$$\tan \theta = \frac{2}{-3}$$

$$\theta = \tan^{-1}\left(-\frac{2}{3}\right)$$

$$= -33.69^\circ \text{ Quad IV}$$

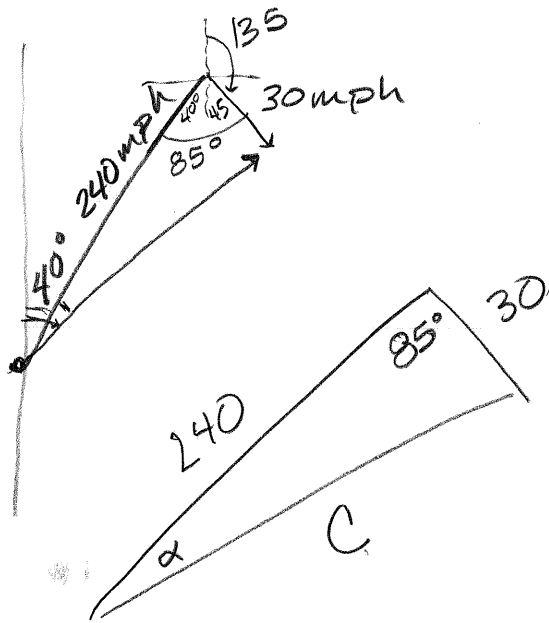
$$180 - 33.69^\circ = 146.31^\circ$$

b) $\vec{A} - \vec{B} = \langle -3-1, 2-4 \rangle$
 $\langle -4, -2 \rangle$

c) $\vec{A} \cdot \vec{B} = (-3)(1) + 2(4)$
 $-3 + 8 = 5$

d) angle between \vec{A} & \vec{B}

$$\cos \alpha = \frac{5}{\sqrt{13} \cdot \sqrt{17}} \Rightarrow \alpha = \cos^{-1}\left(\frac{5}{\sqrt{13} \cdot \sqrt{17}}\right)$$
$$70.346^\circ$$



$$C^2 = 30^2 + 240^2 - 2(30)(240)(\cos 85)$$

$$= 57244.9573$$

$$C = 239.2592 \text{ mph}$$

$$\frac{30 \sin 85}{239.2591844} = \frac{\sin \alpha}{30} \cdot 30$$

$$\alpha = \sin^{-1} \left(\frac{30 \sin 85}{239.2591844} \right)$$

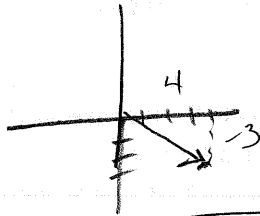
$$\alpha = 7.175552688$$

Bearing: 47.176°
 Speed: 239.259 mph

#23 $z_1 = 4 - 3i$

$z_2 = 3 + 3i$

a) $z_1 = 4 - 3i$



$$r = \sqrt{4^2 + (-3)^2}$$

$$= \sqrt{25}$$

$$= 5$$

$$\tan \theta = \frac{-3}{4}$$

$$\theta = \tan^{-1}\left(\frac{-3}{4}\right)$$

$$\theta = -36.8699$$

360 + ↗

$$323.1301^\circ$$

* $z_1 = 5 \left(\cos 323.1301 + i \sin 323.1301 \right)$

$z_2 = 3 + 3i$

$$r = 3\sqrt{2}$$

$$\tan \theta = \frac{3}{3} = 1$$

* $z_2 = 3\sqrt{2} \left(\cos 45 + i \sin 45 \right)$

$$\theta = \tan^{-1}(1)$$

$$= 45^\circ$$

b) $z_1 z_2 = 5 \cdot 3\sqrt{2} \left[\cos (323.1301 + 45) + i \sin (323.1301 + 45) \right]$

$$= 15\sqrt{2} \left(\cos 368.1301 + i \sin 368.1301 \right)$$

$$= 15\sqrt{2} \left(\cos 8.1301 + i \sin 8.1301 \right)$$

$$\frac{z_2}{z_1} = \frac{3\sqrt{2}}{5} \left(\cos (45 - 323.1301) + i \sin (45 - 323.1301) \right)$$

$$\frac{3\sqrt{2}}{5} \left(\cos -278.1301 + i \sin -278.1301 \right)$$

2+3i

$$\frac{3\sqrt{2}}{5} (\cos 81.87 + i \sin 81.87)$$

$$\frac{3}{25} + \frac{21}{25} i$$

$$c) z_1^4 = 5^4 (\cos 4 \cdot (323.1301) + i \sin 4 \cdot (323.1301))$$

$$d) 3^{\text{rd}} \text{ roots of } z_2 = 3\sqrt{2} (\cos 45 + i \sin 45)$$