

9/24/2012 - Sec 2.3

Math 1060

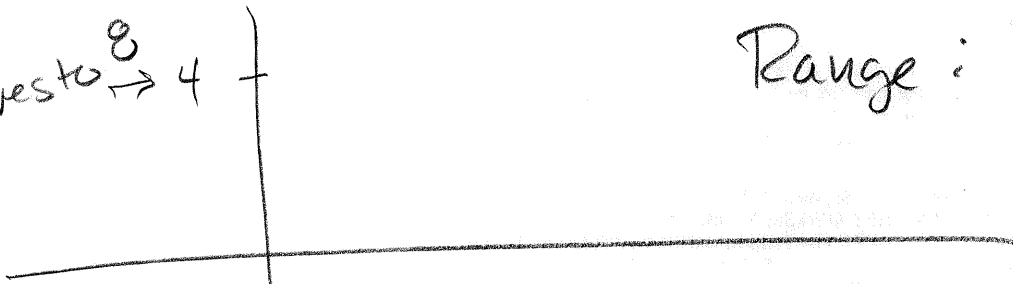
2.2 # 48

Amp = 4

Vertical Shift = 4

Range:  $[0, 8]$

moves to  $\overset{8}{\rightarrow} 4$



b.  $v = -4 \cos(16\pi t) + 4$

frequency =  $\frac{1}{\text{period}}$

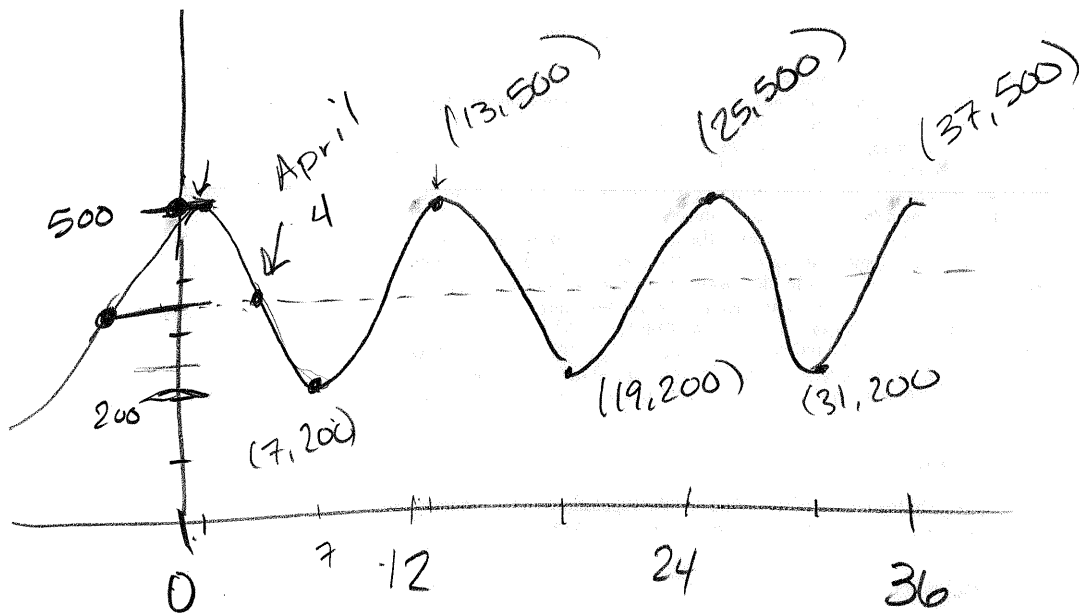
period =  $\frac{2\pi}{B}$

$= \frac{2\pi}{3 \cdot 16\pi} = \frac{1}{3}$

frequency =  $\frac{1}{\frac{1}{3}} = 3 \frac{\text{beats}}{\text{sec}} \cdot \frac{60 \text{ sec}}{1 \text{ min}}$

$= 180 \text{ beats/min}$

#50



Vertical Shift : 350

$$\text{Amp} = 150 = A$$

$$\text{Period} = 12 = \frac{2\pi}{B} \rightarrow \frac{12B}{12} = \frac{2\pi}{12}$$

Phase shift = Right 4

$$B = \frac{\pi}{6}$$

$$y = A \sin [B(x-c)] + D$$

$$y = -150 \sin \left[ \frac{\pi}{6}(x-4) \right] + 350$$

Nov  $\Rightarrow x = 11$

[snow.edu/janakej/1060](http://snow.edu/janakej/1060)

## Sec 2.3 Graphs Secants and Cosecants

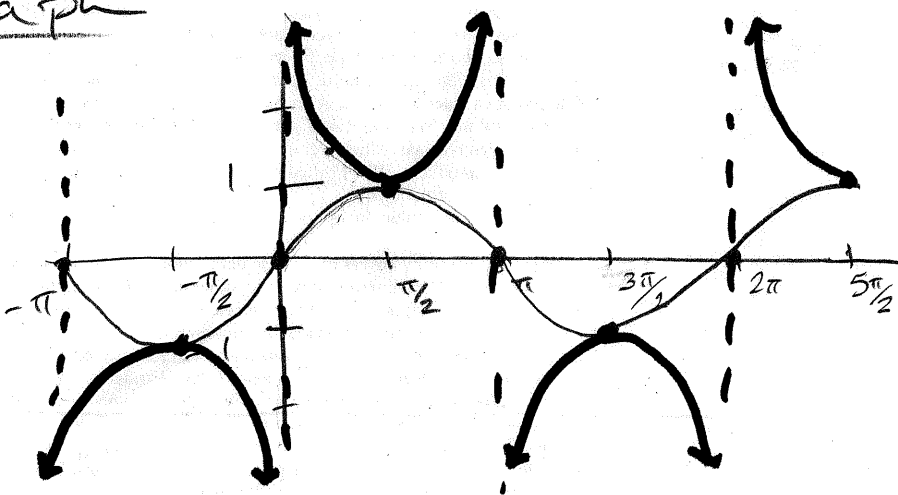
$$\sec \theta = \frac{1}{\cos \theta}$$

$$\csc \theta = \frac{1}{\sin \theta}$$

### Cosecant Graph

1. Graph  $y = \sin x$

$$\begin{aligned} \csc \theta &= \frac{1}{\sin \theta} \\ &= \frac{1}{0} \end{aligned}$$



2. cosecant curve

asymptote when  $\sin x = 0$

$x = k\pi$ , where  $k$  is any integer

3. when  $\sin x = 1$

when  $\sin x = 1$  or  $-1$

$\sin x = -1$

$\csc x = 1$  or  $-1$

4. Examine  $\sin x \rightarrow 0$

### Facts about Cosecant

Period =  $2\pi$  (same as  $y = \sin x$ )

Asymptotes:  $y = k\pi$

Range:  $(-\infty, -1] \cup [1, \infty)$

# General Cosecant

$$y = A \csc[B(x-C)] + D$$

$\uparrow$  Stretch       $\uparrow$  changes period       $\uparrow$  phase shift       $\uparrow$  Vertical

## Graph: $y = 3 \csc[2(x - \frac{\pi}{4})]$

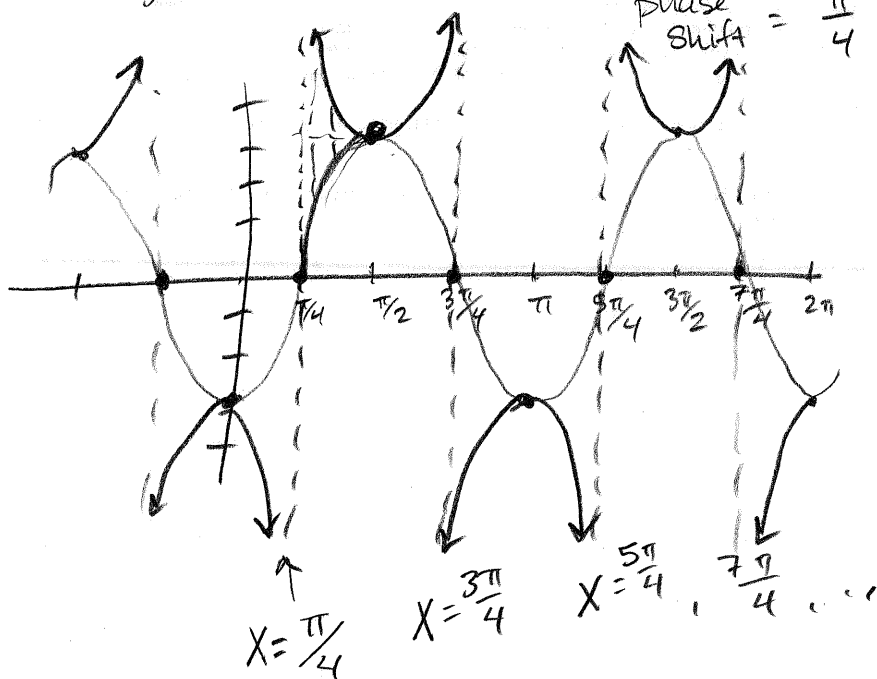
$$y = 3 \sin[2(x - \frac{\pi}{4})]$$

Amp = 3  
 Period =  $\frac{2\pi}{2} = \pi$   
 phase shift =  $\frac{\pi}{4}$

1st Graph the sine curve as a reference

2nd Determine Asymptotes

3rd Graph Cosecant Curve



Period =  $\pi$

Asymptotes:  $x = \frac{\pi}{4} + \frac{\pi}{2}k$

$\uparrow$  phase shift       $\uparrow$  half the period  $\times k$

## Secant

Reference curve as cosine

$$x = \frac{\pi}{2} + \pi k$$