

#30

$$X = -\frac{1}{2}y^2 - 4y - 6$$

Left / Right

$$X = a(y - k)^2 + h$$

Vertex: (2, -4) ✓

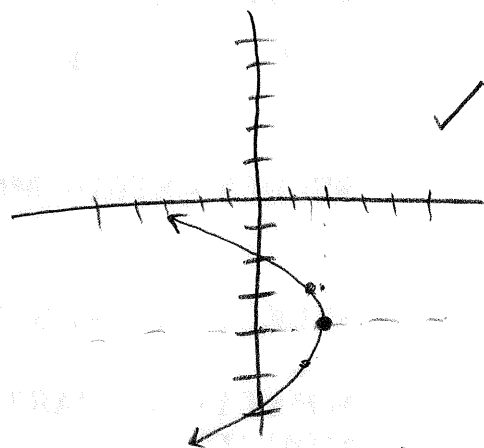
$$y = \frac{-b}{2a} = \frac{-(-4)}{2(-\frac{1}{2})} = \frac{4}{-1} = -4$$

$$X = -\frac{1}{2}(-4)^2 - 4(-4) - 6$$

$$= -\frac{1}{2} \cdot 16 + 16 - 6$$

$$= -8 + 16 - 6$$

$$= 8 - 6 = 2$$



X	y
2	-4
1.5	-3
1.5	-5

axis of symmetry:

$$y = -4$$

Domain:  $(-\infty, 2]$

Range:  $(-\infty, \infty)$

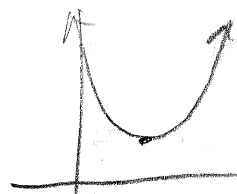
#42

is units

$$C(x) = x^2 - 70x + 1500$$

cost       $a=1$        $b=-70$        $c=1500$

$$X = \frac{-b}{2a} = \frac{-(-70)}{2(1)} = \frac{70}{2} = 35$$



Minimum cost @ Vertex

35 units

Minimum cost:  $C(35)$

= \$275

$$(35)^2 - 70(35) + 1500$$

#45

$$a = -20,57$$

$$b = 758,9$$

$$f(x) = -20,57x^2 + 758,9x - 3140$$

Note:  $x=10 \rightarrow 2010$

$x=15 \rightarrow 2015$

$f(x)$  in Billions of \$

$$x = \frac{-b}{2a} = \frac{-758,9}{2(-20,57)} = 18,45$$

$$f(18,45) = -20,57(18,45)^2 + 758,9(18,45) - 3140 = (18,45, 3860.)$$

$\approx 2018$  the Social Security Assets would be  $\approx \$3860$  billion

# See 11.1 Additional Graphs of Functions

## Recall Parabola

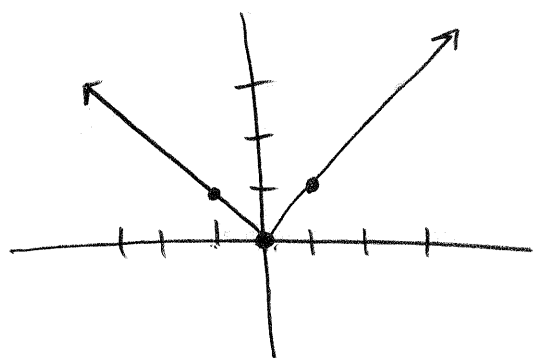
$$f(x) = a(x-h)^2 + k$$

$a$ : stretch  
 $h$ : left/right  
 $k$ : up/down

tells us parent is parabola

## The Absolute Value Function

$$f(x) = |x|$$



Domain:  $(-\infty, \infty)$

Range:  $[0, \infty)$

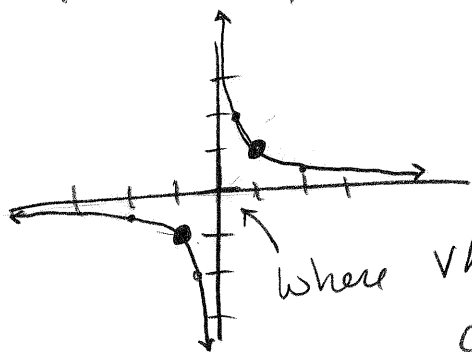
x	y
0	0
1	1
-1	1

## The Reciprocal Function

$$f(x) = \frac{1}{x}$$

VA:  $x=0$

HA:  $y=0$



where VA & HA cross

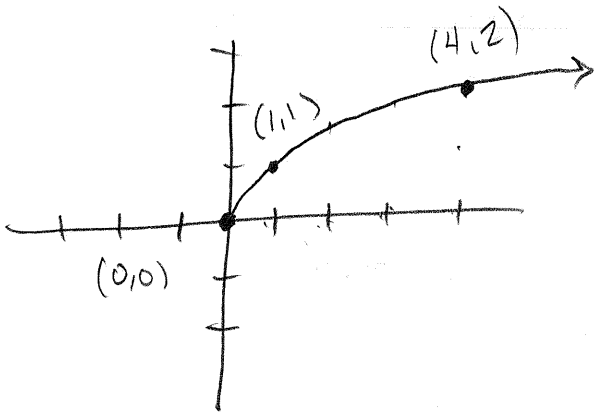
Domain:  $\{x \mid x \neq 0\}$   
 $(-\infty, 0) \cup (0, \infty)$

Range:  $\{y \mid y \neq 0\}$   
 $(-\infty, 0) \cup (0, \infty)$

x	y
0	undefined
1	1
2	$\frac{1}{2}$
$\frac{1}{2}$	$\frac{1}{\frac{1}{2}} = 1 \cdot \frac{2}{1} = 2$
-1	-1
-2	$-\frac{1}{2}$
$-\frac{1}{2}$	-2

# The Square Root Function

$$f(x) = \sqrt{x}$$



Domain:  
[0, ∞)

Range:  
[0, ∞)

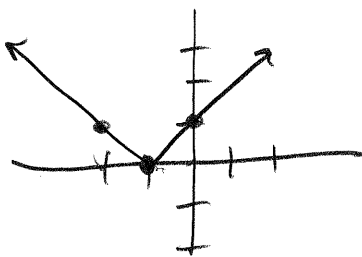
x	y
0	0
1	1
-1	Not Real
4	2

## Moving Parent functions

### Remember

1. Number outside parent function moves up/down
2. Number inside parent function with x moves left/Right (always opposite sign)

# 11  $f(x) = |x + 1|$  ← parent Absolute Value  $\checkmark$   
← -1



Domain: (-∞, ∞)

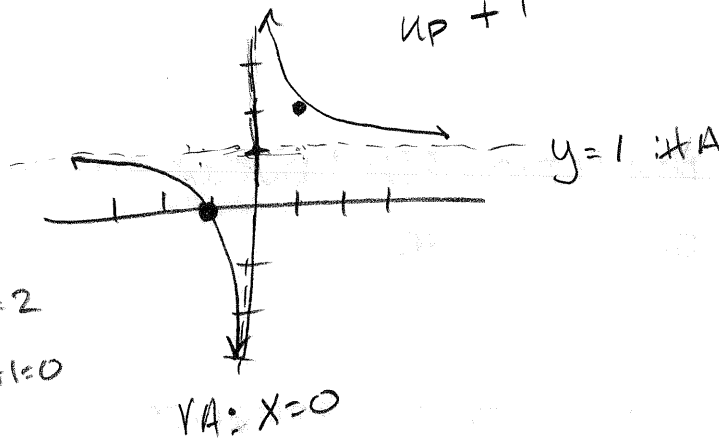
Range: [0, ∞)

#13  $f(x) = \frac{1}{x} + 1$

Reciprocal



↑  
HP + 1



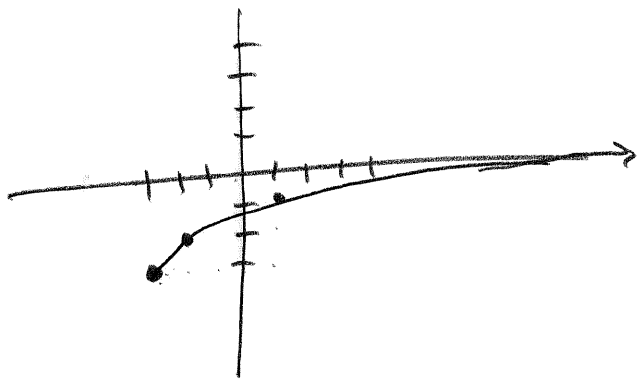
Domain:  $\{x | x \neq 0\}$

Range:  $\{y | y \neq 1\}$

X	y
1	$\frac{1}{1} + 1 = 1 + 1 = 2$
-1	$\frac{1}{-1} + 1 = -1 + 1 = 0$

#19  $f(x) = \sqrt{x + 3} - 3$

Square Root



Domain:  $[-3, \infty)$

Range:  $[-3, \infty)$

X	y
-3	-3
-2	-2
-4	undefined
1	-2