

50

80

75

#50 $3 \cdot \frac{4t}{3 \cdot 9a^8b^7} + \frac{5s}{27a^4b^3} \cdot a^4b^4$ LCD: $27a^8b^7$

$$\frac{12t}{27a^8b^7} + \frac{5sa^4b^4}{27a^8b^7}$$

$$\frac{12t + 5sa^4b^4}{27a^8b^7}$$

75

$$\frac{4}{(x+1)} + \frac{1}{(x^2-x+1)} - \frac{12}{x^3+1}$$

$$\frac{4 \cdot (x^2-x+1)}{(x+1) \cdot (x^2-x+1)} + \frac{1 \cdot (x+1)}{(x^2-x+1) \cdot (x+1)} - \frac{12}{(x+1)(x^2-x+1)}$$

x^2-x+1 ac b

1	-1
+	+
+	2
+	-2

$$\frac{4(x^2-x+1)}{(x+1)(x^2-x+1)} + \frac{(x+1)}{(x+1)(x^2-x+1)} - \frac{12}{(x+1)(x^2-x+1)}$$

LCD: $(x+1)(x^2-x+1)$

$$\frac{4x^2 - 4x + 4 + x + 1 - 12}{(x+1)(x^2-x+1)}$$

Ans

$$\frac{4x-7}{x^2-x+1}$$

$$\left\{ \frac{4x^2 - 3x - 7}{(x+1)(x^2-x+1)} = \frac{(x+1)(4x-7)}{(x+1)(x^2-x+1)} \right.$$

ac	b
-28	-3
4	-7
+	+
+	-3
+	-7
+	-7

$\frac{4}{4} = 1$ $\frac{-7}{4}$

#80

$$\frac{8}{(3r-1)^2} + \frac{2 \cdot (3r-1)}{(3r-1)(3r-1)} - \frac{6(3r-1)^2}{(3r-1)^2} \quad \text{LCD: } (3r-1)^2$$

$$\frac{8}{(3r-1)^2} + \frac{2(3r-1)}{(3r-1)^2} - \frac{6(3r-1)^2}{(3r-1)^2}$$

$$\frac{8 + 6r - 2 - 6(9r^2 - 6r + 1)}{(3r-1)^2}$$

$$\frac{8 + 6r - 2 - 54r^2 + 36r - 6}{(3r-1)^2}$$

$$\frac{-54r^2 + 42r}{(3r-1)^2} = \frac{-6r(9r-7)}{(3r-1)^2}$$

Sec 7.3 Complex Fractions

Defn: A complex fraction is a quotient having a fraction in the numerator, a fraction in the denominator or both

Ex: $\frac{2 + \frac{5}{x}}{3}$, $\frac{5}{\frac{2}{x-1} + 3}$, $\frac{\frac{1}{x} + 3}{x + \frac{2}{x}}$

Goal for simplifying a Complex Fraction: Rewrite as a Single Fraction

Method 1: Flip & multiply Method

Step 1: Simplify the Numerator and the denominator separately (aka single fraction on top, single fraction on bottom)

Step 2: flip and multiply the denominator fraction

Step 3: Simplify the result, if possible

$$\frac{\frac{y+1}{y}}{\frac{y-2}{3y}} = \frac{(y+1) \cdot 3y}{y \cdot (y-2)} = \frac{3(y+1)}{y-2}$$

$$\frac{\frac{2x+3}{1x} \cdot \frac{3}{x}}{\frac{5x}{1x} \cdot \frac{x-1}{x}} = \frac{\frac{2x+3}{x} \cdot 3}{5x \cdot \frac{x-1}{x}} = \frac{\frac{2x+3}{x} \cdot 3}{5(x-1)}$$
$$= \frac{(2x+3) \cdot 3}{x \cdot (5x-5)} = \boxed{\frac{2x+3}{5x-5}}$$

Method #2: LCD Method

Step 1: Find the LCD of Each Fraction in the Numerator and the Denominator

Step 2: Multiply the Numerator and the Denominator by the LCD (aka clear the fractions using LCD)

Step 3: Simplify the Resulting Fraction if possible

Ex: $\frac{2 + \frac{3}{x}}{5 + \frac{x-1}{x}}$ Recall Earlier Ans: $\frac{2x+3}{6x-1}$
LCD: x

$$\begin{aligned} \frac{\left(2 + \frac{3}{x}\right) \cdot x}{\left(5 + \frac{x-1}{x}\right) \cdot x} &= \frac{2x + \frac{3x}{x}}{5x + \frac{(x-1)x}{x}} \\ &= \frac{2x + 3}{5x + (x-1)} \\ &= \frac{2x + 3}{6x - 1} \end{aligned}$$

$$\text{Ex: } \frac{\left(x + \frac{5}{x}\right) \cdot x(x-2)}{\left(4x - \frac{1}{x-2}\right) \cdot x(x-2)}$$

$$\frac{x^2(x-2) + 5(x-2)}{4x^2(x-2) - x}$$

$$\frac{x^2(x-2) + 5(x-2)}{4x^2(x-2) - x}$$

$$\text{LCD: } x(x-2)$$

$$= \frac{(x-2)(x^2+5)}{4x^3 - 8x^2 - x}$$

$$= \frac{(x-2)(x^2+5)}{x(4x^2 - 8x - 1)}$$

ac	b
-4	-8
1+1	0
2-2	0