

# Math 1010 Final Exam Review

## Answer Key

① Solve  $6x - (5x - 1) = 2$

$$6x - 5x + 1 = 2$$

$$x + 1 = 2$$

$$x = 1$$

$$x = 1$$

② Solve  $-8b - 10 = -7 - 6b$

$$+6b \quad +6b$$

$$-2b - 10 = -7$$

$$+10 \quad +10$$

$$-2b = 3$$

$$\frac{-2b}{-2} = \frac{3}{-2}$$

$$b = -\frac{3}{2}$$

$$b = -\frac{3}{2} \text{ or } -1\frac{1}{2}$$

③ Find Slope between  $(-9, -8)$  +  $(4, 9)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{9 - (-8)}{4 - (-9)} = \frac{9 + 8}{4 + 9} = \frac{17}{13}$$

$$m = \frac{17}{13}$$

④ Write  $3x - 6y = 2$  in Slope-intercept Form

$$-3x \quad -3x$$

$$-6y = -3x + 2$$

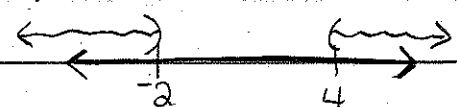
$$\frac{-6y}{-6} = \frac{-3x + 2}{-6}$$

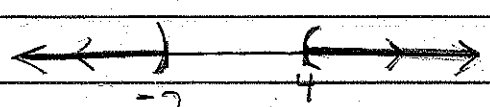
$$y = \frac{1}{2}x - \frac{1}{3}$$

$$y = \frac{1}{2}x - \frac{1}{3}$$

8) Solve. Give Solution in graph & interval notation.

$$\begin{array}{ccc} x-2 > 2 & \text{or} & x+3 < 1 \\ +2 & +2 & -3 & -3 \end{array}$$

$$\begin{array}{ccc} x > 4 & \text{or} & x < -2 \end{array}$$



$$(-\infty, -2) \cup (4, \infty)$$

9) Solve  $|6m+5| = 6$

$$\begin{array}{ccc} 6m+5 = 6 & & 6m+5 = -6 \\ -5 & -5 & -5 & -5 \end{array}$$

$$\begin{array}{ccc} 6m = 1 & & 6m = -11 \\ \frac{6m}{6} & \frac{6m}{6} & \frac{6m}{6} & \frac{-11}{6} \end{array}$$

$$m = \frac{1}{6} \qquad m = -\frac{11}{6}$$

$$\left\{ -\frac{11}{6}, \frac{1}{6} \right\}$$

10) Solve  $5|9x+1| + 3 < 23$

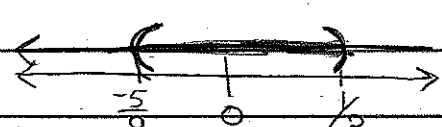
$$\frac{5|9x+1|}{5} < \frac{20}{5}$$


$$|9x+1| < 4$$

$$\begin{array}{ccc} 9x+1 < 4 & \text{and} & 9x+1 > -4 \\ -1 & -1 & -1 & -1 \end{array}$$

$$\frac{9x}{9} < \frac{3}{9} \quad \text{and} \quad \frac{9x}{9} > \frac{-5}{9}$$

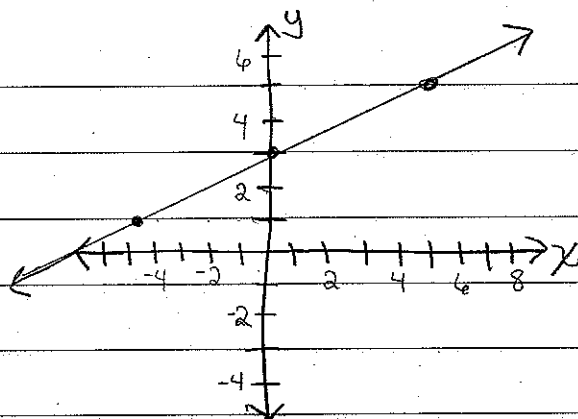
$$x < \frac{1}{3} \quad \text{and} \quad x > -\frac{5}{9}$$




$$\left( -\frac{5}{9}, \frac{1}{3} \right)$$

⑤ Graph  $2x - 5y = -15$

$$\begin{aligned} -2x & & -2x \\ -5y & = -2x - 15 \\ \frac{-5y}{-5} & = \frac{-2x}{-5} - \frac{15}{-5} \\ y & = \frac{2}{5}x + 3 \end{aligned}$$



⑥ Find the midpoint between  $(5, 3)$  +  $(2, 7)$

$$\begin{aligned} M & = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) = \left( \frac{5+2}{2}, \frac{3+7}{2} \right) \\ & = \left( \frac{7}{2}, \frac{10}{2} \right) = \boxed{\left( \frac{7}{2}, 5 \right)} \end{aligned}$$

⑦ Are the lines parallel, perpendicular or neither? (compare slopes)

$$\begin{aligned} 3x - 2y & = -9 \\ -3x & & -3x \end{aligned}$$

$$\frac{-2y}{-2} = \frac{-3x}{-2} - \frac{9}{-2}$$

$$y = \frac{3}{2}x + \frac{9}{2}$$

$$m = \frac{3}{2}$$

$$\begin{aligned} 2x + 3y & = -3 \\ -2x & & -2x \end{aligned}$$

$$\frac{3y}{3} = \frac{-2x}{3} - \frac{3}{3}$$

$$y = -\frac{2}{3}x - 1$$

$$m = -\frac{2}{3}$$

Since the slopes are opposite signs + reciprocals,  
the lines are Perpendicular

⑩ Factor completely  $125x^3 + 27$  Sum of Cubes

$$5^3 = 125 \quad 3^3 = 27$$

$$(5x + 3)(25x^2 - 15x + 9)$$

⑪ Factor completely

$$24m^7 - 20m^5 - 28m^3 \quad \text{GCF}$$

$$4m^3(6m^4 - 5m^2 - 7)$$

$$4m^3(6m^4 - 5m^2 - 7)$$

⑫ Factor Completely

$$x^2 + 16x + 64$$

No GCF

Factors of 64

$$(x+8)(x+8)$$

Add to 16  $\int 8+8$

$$(x+8)^2$$

$$(x+8)^2$$

⑬ Solve the System by Graphing

$$x - y = 6$$

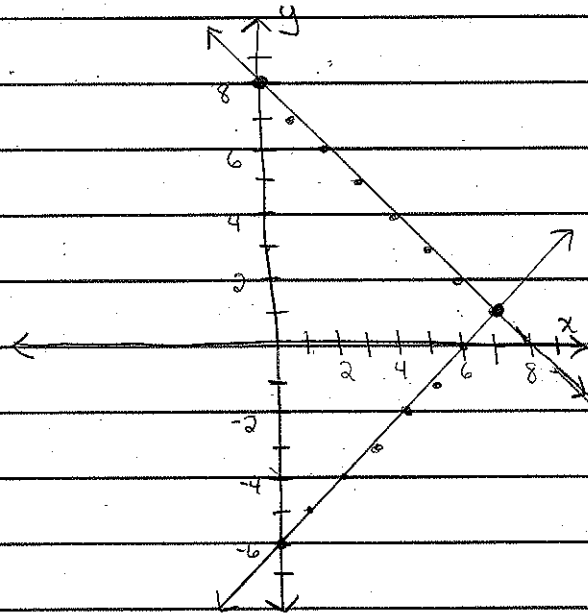
$$x + y = 8$$

$$-y = -x + 6$$

$$y = -x + 8$$

$$y = x - 6$$

Solution  $(7, 1)$



⑪ Simplify  $(-4p)^2 (-4p)^6$

$$4^2 p^2 \cdot 4^6 p^6$$

$$4^8 p^8$$

$$\boxed{4^8 p^8}$$

⑫ Simplify  $\left(\frac{3p^3 v^4}{s^4}\right)^2$

$$\frac{3^2 p^6 v^8}{s^8}$$

$$\boxed{\frac{3^2 p^6 v^8}{s^8}}$$

⑬  $(3p-1)(9p^2+3p+1)$

$$\begin{array}{r} 27p^3 + 9p^2 + 3p \\ -9p^2 - 3p - 1 \\ \hline 27p^3 - 1 \end{array}$$

$$\boxed{27p^3 - 1}$$

⑭  $(-6x^3 + 9x^2 + 4) - (-5x^3 + 2x - 5)$

$$\begin{array}{r} -6x^3 + 9x^2 + 4 + 5x^3 - 2x + 5 \\ -1x^3 + 9x^2 - 2x + 9 \end{array}$$

$$\boxed{-x^3 + 9x^2 - 2x + 9}$$

⑮  $x-7$

$$\begin{array}{r} x+9 \overline{) x^2 + 2x - 63} \\ \underline{\ominus x^2 + 9x} \phantom{-63} \\ -7x - 63 \\ \underline{\oplus 7x + 63} \\ 0 \end{array}$$

$$\boxed{x-7}$$

20

Solve by substitution

$$x - 6y = 24$$

$$-7x - 7y = -21$$

$$x = 6y + 24$$

$$-7(6y + 24) - 7y = -21$$

$$x = 6(-3) + 24$$

$$-42y - 168 - 7y = -21$$

$$x = -18 + 24$$

$$-49y - 168 = -21$$

$$x = 6$$

$$\begin{array}{r} -49y = 147 \\ \underline{-49} \quad \underline{-49} \end{array}$$

$$y = -3$$

Solve by Elimination

$$x - 6y = 24$$

$$\times 7 = 7x - 42y = 168$$

$$-7x - 7y = -21$$

$$\underline{-7x - 7y = -21}$$

$$x - 6y = 24$$

$$\begin{array}{r} -49y = 147 \\ \underline{-49} \quad \underline{-49} \end{array}$$

$$x - 6(-3) = 24$$

$$y = -3$$

$$\begin{array}{r} x + 18 = 24 \\ \underline{-18} \quad \underline{-18} \end{array}$$

(6, -3)

$$x = 6$$

21

$$\text{Jill} + \text{Joe} = 20$$

$$(2.5)(5) + (x)(5) = 20$$

$$12.5 + 5x = 20$$

$$\begin{array}{r} -12.5 \\ \underline{-12.5} \end{array}$$

$$5x = 7.5$$

$$x = 1.5$$

Joe walked @  
1.5 mph

$$\textcircled{22} \quad \$5 \text{ bills} + \$20 \text{ bills} = \$775$$

$$(5)(x) + (20)(x+5) = 775$$

$$5x + 20x + 100 = 775$$

$$25x + 100 = 775$$

$$25x = 675$$

$$x = 27$$

27 \$5 bills

$$\textcircled{23} \quad 12\% + 8\% = 8000$$

$$(.12)(x) + (.08)(70000 - x) = 8000$$

$$.12x + 5,600 - .08x = 8000$$

$$.04x + 5,600 = 8000$$

$$.04x = 2,400$$

$$x = 60,000$$

She invested  
\$60,000 @ 12%

$$\textcircled{24} \quad 40\% + 90\% = 60\%$$

$$(.4)(x) + (.9)(20) = .6(x+20)$$

$$.4x + 18 = .6x + 12$$

$$-.6x \quad \quad \quad -.6x$$

$$-.2x + 18 = 12$$

$$-18 \quad \quad -18$$

$$-.2x = -6$$

$$x = 30$$

30 liters of  
40% solution

(25)

$$s = \frac{1}{2}at^2 + v_0t + s_0$$

$$v_0 = 400 \text{ ft/sec}$$

$$s_0 = 0$$

$$a = -32 \text{ ft/sec}^2$$

$$s = 2500$$

$$2500 = \frac{1}{2}(-32)t^2 + 400t + 0$$

$$2500 = -16t^2 + 400t$$

$$+16t^2 - 400t + 16t^2 - 400t$$

$$16t^2 - 400t + 2500 = 0$$

$$4(4t^2 - 100t + 625) = 0$$

$$t = \frac{-(-100) \pm \sqrt{100^2 - 4(4)(625)}}{2(4)} = \frac{100 \pm \sqrt{10,000 - 10,000}}{8}$$

$$= \frac{100}{8} = 12.5$$

12.5 sec

(26)

$$\text{Simplify } \sqrt[3]{9x} \cdot \sqrt[3]{49y}$$

$$= \sqrt[3]{441x^2}$$

$\sqrt[3]{441x^2}$

(27)

$$\text{Simplify } \sqrt[3]{1000x^4y^5}$$

$$= \sqrt[3]{10^3x^4y^5}$$

$$= 10xy \sqrt[3]{xy^2}$$

$$\begin{array}{c} 1000 \\ \uparrow \\ 100 \quad 10 \\ \uparrow \\ 10 \quad 10 \end{array}$$

$10xy \sqrt[3]{xy^2}$

(28)

$$\text{Simplify } \sqrt{5x} + 7\sqrt{80x} + 2\sqrt{180x}$$

$$\begin{array}{c} 8 \cdot 10 \\ \uparrow \quad \uparrow \\ 2 \cdot 4 \cdot 2 \cdot 5 \\ \uparrow \quad \uparrow \\ 2 \cdot 2 \end{array}$$

$$\begin{array}{c} 18 \cdot 10 \\ \uparrow \quad \uparrow \\ 9 \cdot 2 \cdot 2 \cdot 5 \\ \uparrow \quad \uparrow \\ 3 \cdot 3 \end{array}$$

$$1\sqrt{5x} + 28\sqrt{5x} + 12\sqrt{5x}$$

$$41\sqrt{5x}$$

$41\sqrt{5x}$

$$(29) (\sqrt{3x} + 3)(\sqrt{7x} - 3)$$

$$\sqrt{21}x^2 - 3\sqrt{3x} + 3\sqrt{7x} - 9$$

$$x\sqrt{21} - 3\sqrt{3x} + 3\sqrt{7x} - 9$$

$$x\sqrt{21} - 3\sqrt{3x} + 3\sqrt{7x} - 9$$

$$(30) \frac{3}{(9-\sqrt{2})} \frac{(9+\sqrt{2})}{(9+\sqrt{2})}$$

$$= \frac{3(9+\sqrt{2})}{81+9\sqrt{2}-9\sqrt{2}-\sqrt{4}}$$

$$= \frac{3(9+\sqrt{2})}{81-2} = \frac{3(9+\sqrt{2})}{79} = \frac{27+3\sqrt{2}}{79}$$

$$= \frac{3(9+\sqrt{2})}{81-2} = \frac{3(9+\sqrt{2})}{79} = \frac{27+3\sqrt{2}}{79}$$

(31) Write  $5x - 6y = 5$  in function notation  
 $y$  is the dependant variable

$$5x - 6y = 5$$

$$-6y = -5x + 5$$

$$\frac{-6y}{-6} = \frac{-5x + 5}{-6}$$

$$y = \frac{5}{6}x - \frac{5}{6}$$

$$f(x) = \frac{5}{6}x - \frac{5}{6}$$

$$(32) \{(-1, 7) (1, -9) (4, -9) (7, -5) (10, -3)\}$$

The relation is a function because none of the inputs<sup>(x)</sup> has more than 1 output (y).

yes

(33) The graph is NOT a function because it fails the vertical line test.

NO

(34) Solve  $x^2 + 5x - 24 = 0$        $24 = 3 \cdot 8$   
 $(x - 3)(x + 8) = 0$        $-3 + 8 = 5$

$x - 3 = 0$      $x + 8 = 0$   
 $x = 3$        $x = -8$

$\{-8, 3\}$

(35) Solve  $\sqrt{8x + 9} = 9$

$(\sqrt{8x + 9})^2 = 9^2$

$8x + 9 = 81$   
 $-9 \quad -9$

$8x = 72$   
 $x = 9$

$x = 9$

Check  $\sqrt{8(9) + 9} = 9 ?$

$\sqrt{72 + 9} = 9$

$\sqrt{81} = 9 \quad \checkmark$

(36) Solve  $2n^2 = -10n - 7$

$2n^2 + 10n + 7 = 0$

$14 = 2 \cdot 7 = 9$  Does not  
 $1 \cdot 10 = 11$  Factor

Quadratic Formula

$n = \frac{-10 \pm \sqrt{10^2 - 4(2)(7)}}{2(2)}$

$= \frac{-10 \pm \sqrt{100 - 56}}{4}$

$= \frac{-10 \pm \sqrt{44}}{4} = \frac{-10 \pm 2\sqrt{11}}{4} = \frac{2(-5 \pm \sqrt{11})}{4} =$

$\frac{-5 \pm \sqrt{11}}{2}$

37

Solve

$$\frac{x}{16} - \frac{3}{8} = \frac{x-8}{8}$$

$$16 \cdot \frac{x}{16} - \frac{3 \cdot 16}{8} = \frac{(x-8) \cdot 16}{8}$$

$$x - 3 \cdot 2 = 2(x-8)$$

$$x - 6 = 2x - 16$$

$$-2x \quad -2x$$

$$-x - 6 = -16$$

$$+6 \quad +6$$

$$-x = -10$$

$$x = 10$$

$$x = 10$$

38

Solve

$$\frac{-5x}{2x+12} = \frac{2x}{4x+24} + \frac{6x-1}{x+6}$$

common denominator

$$2(x+6) \quad 4(x+6) \quad (x+6) \quad 4(x+6)$$

$$\frac{-5x \cdot 2}{2(x+6) \cdot 2} = \frac{2x}{4(x+6)} + \frac{(6x-1) \cdot 4}{(x+6) \cdot 4}$$

$$-10x = 2x + 24x - 4$$

$$-10x = 26x - 4$$

$$-26x \quad -26x$$

$$-36x = -4$$

$$\frac{-36}{-36} \quad \frac{-4}{-36}$$

$$x = \frac{1}{9}$$

$$x = \frac{1}{9}$$

39) Solve  $3^x = 81$

$$3^x = 3^4$$

$$\begin{array}{c} 81 \\ \wedge \\ 9 \cdot 9 \\ \wedge \quad \wedge \\ 3 \cdot 3 \quad 3 \cdot 3 \end{array}$$

$$x = 4$$

$$\boxed{x = 4}$$

40) Solve  $4^{(1+2x)} = 64$

$$4^{(1+2x)} = 4^3$$

$$\begin{array}{c} 64 \\ \wedge \\ 4 \cdot 16 \\ \quad \wedge \\ \quad 4 \cdot 4 \end{array}$$

$$\begin{array}{r} 1+2x = 3 \\ -1 \quad -1 \end{array}$$

$$2x = 2$$

$$x = 1$$

$$\boxed{x = 1}$$

41) Solve  $\log_3 x = 2$

$$3^2 = x$$

$$9 = x$$

$$\boxed{x = 9}$$

42) Solve  $\log_{125} x = \frac{1}{3}$

$$125^{1/3} = x$$

$$\sqrt[3]{125} = x$$

$$5^{\wedge} 25$$

$$5 \cdot 5$$

$$\sqrt[3]{5 \cdot 5 \cdot 5} = x$$

$$\boxed{x = 5}$$

$$5 = x$$

43

Solve by completing the square

$$x^2 + 8x = 7$$

$$8 \div 2 = 4$$

$$4^2 = 16$$

$$x^2 + 8x + 16 = 7 + 16$$

$$(x + 4)^2 = 23$$

$$\sqrt{(x + 4)^2} = \pm \sqrt{23}$$

$$x + 4 = \pm \sqrt{23}$$

$$x = -4 \pm \sqrt{23}$$

$$x = -4 + \sqrt{23}$$

$$x = -4 - \sqrt{23}$$

44

Solve by completing the square

$$x^2 + x + 5 = 0$$

$$1 \div 2 = \frac{1}{2}$$

$$\left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

$$x^2 + x + \frac{1}{4} = -5 + \frac{1}{4}$$

$$\left(x + \frac{1}{2}\right)^2 = \frac{-19}{4}$$

$$-\frac{20}{4} + \frac{1}{4} = \frac{-19}{4}$$

$$\sqrt{\left(x + \frac{1}{2}\right)^2} = \pm \sqrt{\frac{-19}{4}}$$

$$x + \frac{1}{2} = \pm \frac{\sqrt{-19}}{\sqrt{4}}$$

$$x + \frac{1}{2} = \pm \frac{i\sqrt{19}}{2}$$

$$-\frac{1}{2} \quad -\frac{1}{2}$$

$$x = -\frac{1}{2} \pm \frac{i\sqrt{19}}{2}$$

$$x = -\frac{1}{2} + \frac{\sqrt{19}}{2} i$$

$$x = -\frac{1}{2} - \frac{\sqrt{19}}{2} i$$

45) Use discriminant to decide solutions

$$v^2 + 7v + 1 = 0$$

$$\begin{aligned} b^2 - 4ac &= 7^2 - 4(1)(1) \\ &= 49 - 4 \\ &= 45 \end{aligned}$$

Since 45 is positive but not a perfect square,  
the equation has two irrational solutions.

46) Use the discriminant to decide solutions

$$w^2 - 2w + 8 = 0$$

$$\begin{aligned} b^2 - 4ac &= (-2)^2 - 4(1)(8) \\ &= 4 - 32 \\ &= -28 \end{aligned}$$

Since  $b^2 - 4ac$  is  
negative the equation

has two complex  
solutions

47) What is the vertex of  $y = x^2 + 4x + 13$

$$x \text{ coordinate} = \frac{-b}{2a} = \frac{-4}{2(1)} = \frac{-4}{2} = -2$$

$$\begin{aligned} y \text{ coordinate} &= (-2)^2 + 4(-2) + 13 \\ &= 4 - 8 + 13 \\ &= 9 \end{aligned}$$

The vertex  
is at  
(-2, 9)

48) Graph  $f(x) = 2x^2 - 2x - 5$

Vertex:  $x = \frac{-b}{2a} = \frac{-(-2)}{2(2)} = \frac{2}{4} = \frac{1}{2}$

$$y = 2\left(\frac{1}{2}\right)^2 - 2\left(\frac{1}{2}\right) - 5$$

$$= 2 \cdot \frac{1}{4} - \frac{2}{2} - \frac{10}{2}$$

$$= \frac{1}{2} - \frac{2}{2} - \frac{10}{2} = \frac{-11}{2}$$

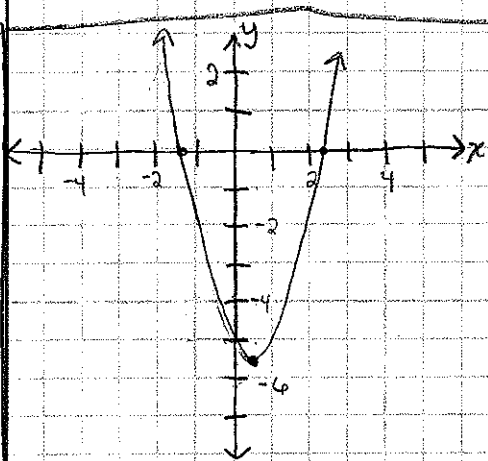
x-intercepts

$$2x^2 - 2x - 5 = 0$$

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(2)(-5)}}{2(2)}$$

$$= \frac{2 \pm \sqrt{44}}{4}$$

$$\approx 2.2, -1.2$$



vertex:  $\left(\frac{1}{2}, -\frac{11}{2}\right)$

axis of symmetry:  $x = \frac{1}{2}$

domain:  $(-\infty, \infty)$

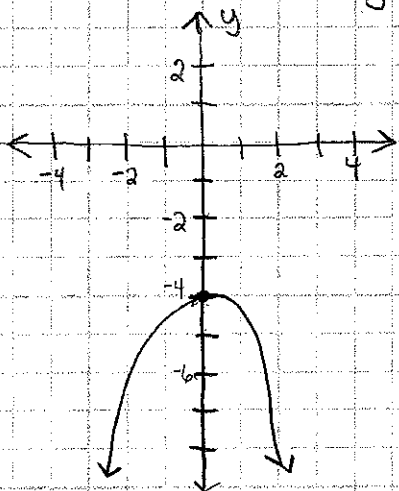
range:  $\left[-\frac{11}{2}, \infty\right)$

49) Graph  $y = -x^2 - 4$

vertex:  $x = \frac{-b}{2a} = \frac{-0}{2(-1)} = 0$

$$y = -0^2 - 4 = -4$$

opens down with vertex below x-axis  
there are no x-intercepts



vertex:  $(0, -4)$

axis of symmetry:  $x = 0$

domain:  $(-\infty, \infty)$

range:  $(-\infty, -4]$

50 SHEETS — 5 SQUARES  
100 SHEETS — 5 SQUARES  
200 SHEETS — 5 SQUARES  
200 SHEETS — FILLER  
COMET

50) Find  $f(4)$  when  $f(x) = x^2 - 4x + 2$

$$\begin{aligned} f(4) &= (4)^2 - 4(4) + 2 \\ &= 16 - 16 + 2 \\ &= 2 \end{aligned}$$

$$f(4) = 2$$

51) Find  $f(-4)$  when  $f(x) = 5x^2 + 2x + 5$

$$\begin{aligned} f(-4) &= 5(-4)^2 + 2(-4) + 5 \\ &= 5(16) - 8 + 5 \\ &= 80 - 8 + 5 \\ &= 72 + 5 \\ &= 77 \end{aligned}$$

$$f(-4) = 77$$

52) Find  $(f-g)(x)$  for  $f(x) = 4x - 3$  &  $g(x) = -9x + 9$

$$(4x - 3) - (-9x + 9) = 4x - 3 + 9x - 9 = 13x - 12$$

53) Find  $(fg)(x)$  for  $f(x) = 4x + 2$  &  $g(x) = -2x - 8$

$$\begin{aligned} (4x + 2)(-2x - 8) &= -8x^2 - 32x - 4x - 16 \\ &= -8x^2 - 36x - 16 \end{aligned}$$

$$-8x^2 - 36x - 16$$

54) Find  $\left(\frac{f}{g}\right)(x)$  for  $f(x) = x^2 + 9x + 20$  &  $g(x) = x + 5$

$$\frac{x^2 + 9x + 20}{x + 5} = \frac{(x + 4)(x + 5)}{x + 5} = x + 4$$

$$x + 4$$

55) find  $(f \circ g)(x)$  for  $f(x) = x + 7$  &  $g(x) = 8x - 2$

$$(f \circ g)(x) = (8x - 2) + 7 = 8x + 5$$

$$\boxed{8x + 5}$$

56)  $(3 - 4i) + (6 + 7i)$

$$= 9 + 3i$$

$$\boxed{9 + 3i}$$

57)  $(8 - 3i)(3 + 2i)$

$$24 + 16i - 9i - 6i^2$$

$$24 + 7i - 6(-1)$$

$$24 + 6 + 7i$$

$$30 + 7i$$

$$\boxed{30 + 7i}$$

58)  $\frac{(6 + 2i)(9 + 3i)}{(9 - 3i)(9 + 3i)}$

$$\frac{54 + 18i + 18i + 6i^2}{81 - 9i^2}$$

$$\frac{54 + 36i + 6(-1)}{81 - 9(-1)}$$

$$\frac{48 + 36i}{90}$$

$$= \frac{48}{90} + \frac{36}{90}i$$

$$= \frac{8}{15} + \frac{2}{5}i$$

$$= \frac{48}{90} + \frac{36}{90}i = \frac{48}{90} + \frac{36}{90}i = \frac{8}{15} + \frac{2}{5}i = \boxed{\frac{8}{15} + \frac{2}{5}i}$$

59)  $i^{21} = i^{20} \cdot i = (i^2)^{10} \cdot i$

$$= (-1)^{10} \cdot i$$

$$= 1 \cdot i$$

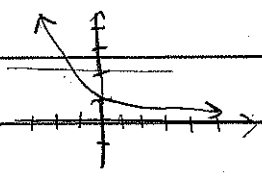
$$= i$$

$$\boxed{i}$$

(60)

is the function one-to-one?

Yes

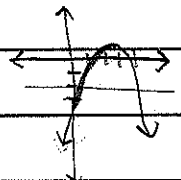


passes the horizontal line test

(61)

is the function one-to-one?

NO



fails the horizontal line test.

(62)

write in lowest terms

$$\frac{2x+2}{10x^2+16x+6} = \frac{2(x+1)}{2(5x^2+8x+3)}$$

$$= \frac{2(x+1)}{2(x+1)(5x+3)}$$

$$= \boxed{\frac{1}{5x+3}}$$

Side work

$$5x^2+8x+3 \quad \begin{array}{l} 3 \cdot 5 = 15 \\ 3+5 = 8 \end{array}$$

$$= 5x^2+5x+3x+3$$

$$= 5x(x+1)+3(x+1)$$

$$= (x+1)(5x+3)$$

(63)

$$\frac{y^2+8y+12}{y^2+14y+48}$$

$$= \frac{(y+6)(y+2)}{(y+6)(y+8)}$$

$$= \boxed{\frac{y+2}{y+8}}$$

Side work

$$6 \cdot 2 = 12$$

$$6+2 = 8$$


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$$6 \cdot 8 = 48$$

$$6+8 = 14$$

(64)

$$\frac{2p-2}{p} \cdot \frac{7p^2}{4p-4}$$

$$\frac{\cancel{2}(p-1)}{p} \cdot \frac{7p^{\cancel{2}}}{\cancel{4}(p-1)}$$

$$\frac{7p}{2}$$

$7p$
$2$

(65)

$$\frac{8r-24s}{3r-6s} \cdot \frac{12s-4r}{2r-4s}$$

$$\frac{\cancel{2}\cancel{8}(r-3s)}{3(\cancel{r}-2s)} \cdot \frac{\cancel{2}(r-2s)}{\cancel{4}(3s-r)}$$

$$\frac{4(r-3s)}{3(3s-r)} = \frac{4(-1)(\cancel{3s-r})}{3(3s-r)} = \frac{-4}{3}$$

$-4$
$3$

(66)

$$\frac{7x+7}{x} + \frac{3x-5}{7x}$$

$$\frac{7 \cdot (7x+7)}{7 \cdot x} + \frac{3x-5}{7x}$$

$$\frac{49x+49 + 3x-5}{7x}$$

$$\frac{52x+44}{7x}$$

$52x+44$
$7x$

(67)

$$\frac{4x}{x+6} + \frac{2}{x-6}$$

$$\frac{4x(x-6)}{(x+6)(x-6)} + \frac{2(x+6)}{(x-6)(x+6)}$$

$$\frac{4x^2 - 24x + 2x + 12}{(x+6)(x-6)}$$

$$\boxed{\frac{4x^2 - 22x + 12}{(x+6)(x-6)}}$$

$$\frac{4x^2 - 22x + 12}{(x+6)(x-6)}$$

also

$$\frac{2(ax^2 - 11x + 6)}{(x+6)(x-6)}$$

(68)

$$\frac{2m^7n^2}{5m}$$

$$\frac{9m^3n^8}{4n^4}$$

$$\frac{2m^7n^2}{5m} \div \frac{9m^3n^8}{4n^4}$$

$$\frac{2m^7n^2}{5m} \cdot \frac{4n^4}{9m^3n^8}$$

$$\frac{8m^7n^6}{45m^4n^8}$$

$$\frac{8m^3}{45n^2}$$

$$\boxed{\frac{8m^3}{45n^2}}$$

(69) find the inverse of  $f(x) = 8x + 5$

$$y = 8x + 5$$

① replace  $f(x)$  with  $y$

$$x = 8y + 5$$

② swap  $x + y$

$$-5 \quad -5$$

③ solve for  $y$

$$\frac{x-5}{8} = \frac{8y}{8}$$

$$\frac{x-5}{8} = y$$

④ replace  $y$  with  $f^{-1}(x)$

$$f^{-1}(x) = \frac{x-5}{8}$$

$$f^{-1}(x) = \frac{x-5}{8}$$

(70) write  $2^3 = 8$  in logarithmic form

$$\log_2 8 = 3$$

$$\log_2 8 = 3$$

(71) write  $\log_{14} 1 = 0$  in exponential form

$$14^0 = 1$$

$$14^0 = 1$$

(72) Choose the correct graph of

$$f(x) = 3^x$$

A

The graph rises from left to right above the  $x$ -axis, because the base is a positive whole number

(73) Choose the correct graph of

$$f(x) = \left(\frac{1}{4}\right)^x$$

D

The graph falls from left to right above the  $x$ -axis because the base is a positive fraction

74

Choose the correct graph of

$$y = \log_4 x$$

A

The graph rises on the right side of the y-axis from below the x-axis to above it because the base is a positive whole number.

75

Choose the correct graph of

$$y = \log_{\frac{1}{8}} x$$

D

The graph falls on the right side of the y-axis from above the x-axis to below it because the base is a positive fraction.