

if α is obtuse

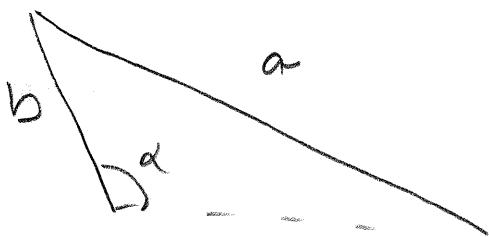
Case 1



← doesn't reach
No triangle

$$a \leq b$$

Case 2



Exactly one triangle $a > b$

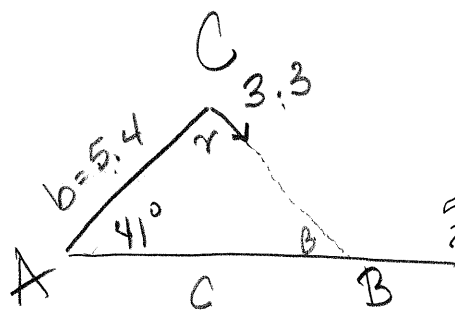
Example:

$$\alpha = 41^\circ, a = 3.3, \text{ and } b = 5.4$$

Solve the triangle: $B = ?$

$\gamma =$

$c =$



$$\frac{5.4}{5.4} \cdot \frac{\sin B}{5.4} = \frac{\sin 41^\circ \cdot 5.4}{3.3}$$

$$\sin B = \frac{(\sin 41^\circ) 5.4}{3.3}$$

$$\sin B = 1.07 \leftarrow \text{NOT possible}$$

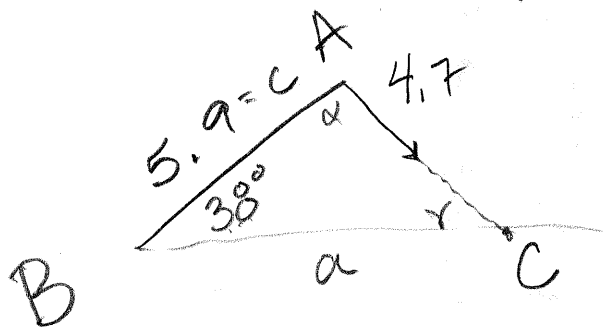
$$B = \sin^{-1}(\quad)$$

No triangle possible

Ex: $\beta = 38^\circ$, $b = 4.7$, $c = 5.9$

Solve the triangle

$\alpha = ?$, $\gamma = ?$, $a = ?$



$$\frac{\sin \gamma}{5.9} = \frac{\sin 38^\circ \cdot 5.9}{4.7}$$

$$\sin \gamma = \frac{(\sin 38^\circ) 5.9}{4.7}$$

$$\sin \gamma = .77285$$

$$\gamma = 50.6^\circ, 129.4^\circ$$

triangle 1 ✓

$$\gamma = 50.6^\circ$$

$$\beta = 38^\circ$$

$$\alpha = 180^\circ - (50.6 + 38) = 91.4^\circ$$

$$\frac{a}{\sin 91.4} = \frac{4.7}{\sin 38}$$

$$a = \frac{4.7(\sin 91.4)}{\sin 38} = 7.6318$$

triangle 2 ✓

$$\gamma = 129.4^\circ$$

$$\beta = 38^\circ$$

$$\alpha = 180 - (129.4 + 38) = 12.6^\circ$$

$$\frac{a}{\sin 12.6} = \frac{4.7}{\sin 38}$$

$$a = \frac{4.7 \sin 12.6}{\sin 38} = 1.6653$$

Ans

Triangle 1

$$\gamma = 50.6^\circ$$

$$\alpha = 91.4^\circ$$

$$a = 7.6318$$

Triangle 2

$$\gamma = 129.4^\circ$$

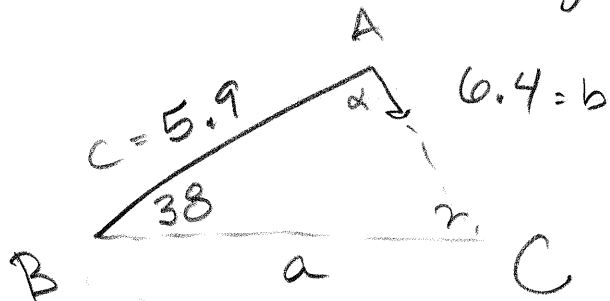
$$\alpha = 12.6^\circ$$

$$a = 1.6653$$



Ex: $B = 38^\circ$, $b = 6.4$, $c = 5.9$

Solve the triangle: $\alpha = ?$, $a = ?$, $\gamma = ?$



$$5.9 \cdot \frac{\sin 38}{6.4} = \frac{\sin \gamma}{5.9} \cdot 5.9$$

$$\frac{5.9 \sin 38}{6.4} = \sin \gamma$$

$$.5676 = \sin \gamma$$

$$34.6 = \gamma$$

Ans

$$\alpha = 107.4^\circ$$

$$\gamma = 34.6^\circ$$

$$a = 9.9$$

Triangle 1

$$\gamma = 34.6^\circ$$

$$B = 38^\circ$$

$$\alpha = 180^\circ - (34.6^\circ + 38^\circ)$$

$$= 107.4$$

~~$$\frac{a}{\sin 107.4} = \frac{6.4}{\sin 38} \cdot \sin 107.4$$~~

~~$$a = \frac{6.4 \sin 107.4}{\sin 38} = \frac{19.49}{9.9}$$~~

~~Triangle 2~~

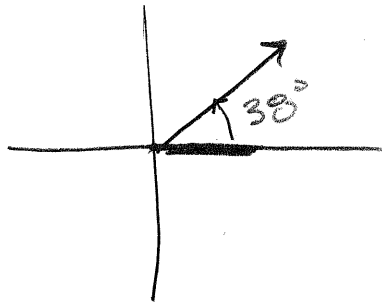
~~$$\gamma = 145.4$$~~

~~$$B = 38^\circ$$~~

~~$$\alpha = 180 - (145.4 + 38)$$~~
~~$$= -3.4$$~~

In Math

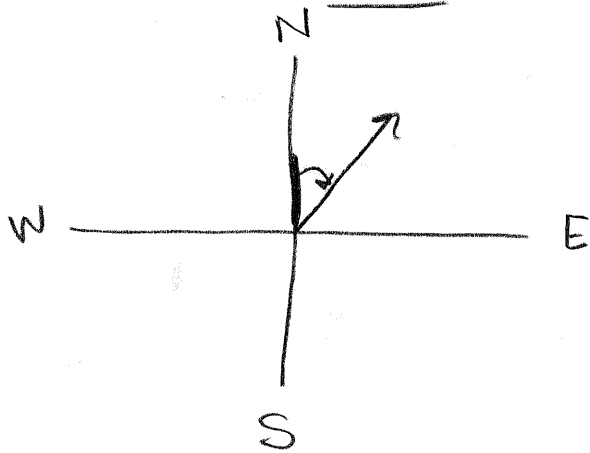
38°



Bearing :

1st

a positive angle between 0 and 360° measured clockwise from due North

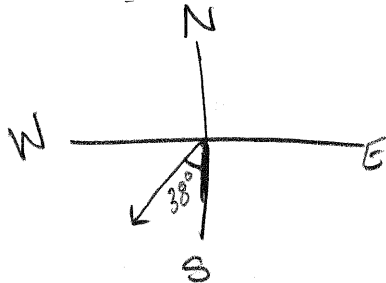


Bearing of 38°

2nd

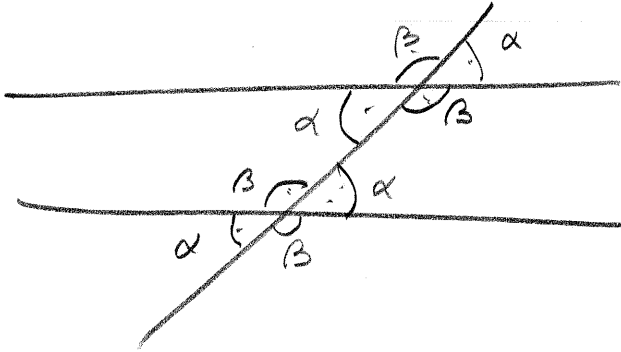
Start at North line or South line and move the acute angle in the specified Direction

Ex: S 38° W



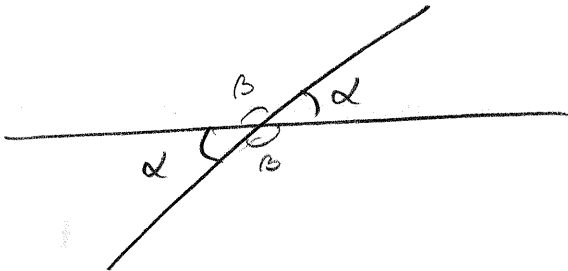
Geometry Property

* Z-prop (AIA ^{alternate interior} angles)



← only if
// lines

* Vertical Angles



←