

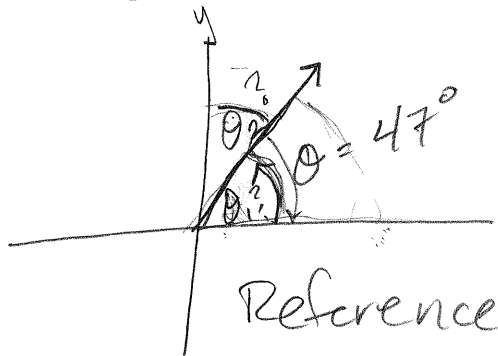
Sec 1.6

Sec 2.1

Example of a Reference Angle:

$\theta = 47^\circ$

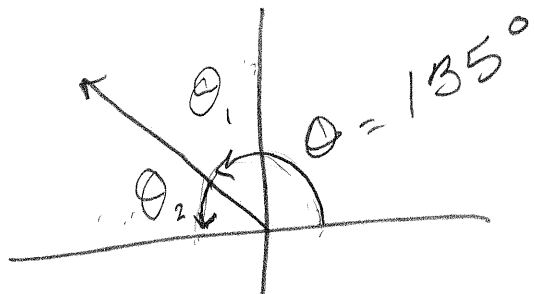
Defn: terminal side  
to closest X-axis



Reference angle =  $\theta_1 = \theta = 47^\circ$

$\theta$  in Quad I,  $\theta = \theta'$

$\theta = 135^\circ$



$\theta_2$  is Reference Angle

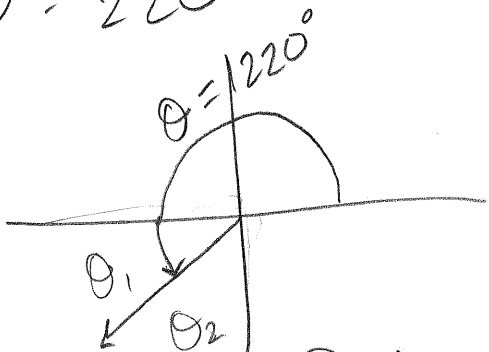
$180 - 135^\circ = 45^\circ$

$\theta$  in Quad II,  $\theta' = 180^\circ - \theta$   
in Radians

$\theta' = \pi - \theta$

$\theta = 220^\circ$

$\theta_1$  is Reference angle



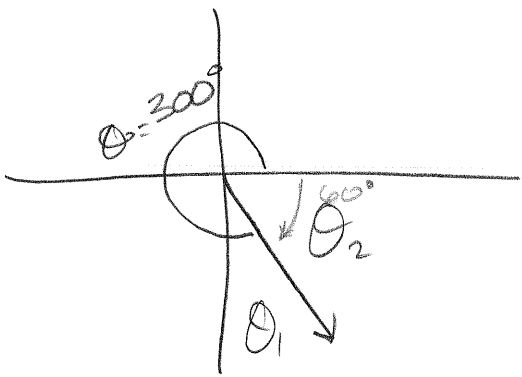
$180 - 220 = -40$

Positive Reference angle  $| -40 | = 40$

or  $220 - 180 = 40$

$\theta$  in Quad III,  $\theta' = \theta - 180^\circ$   
 $\theta' = \theta - \pi$  in Rads

$$\theta = 300^\circ$$



$\theta_2$  is reference angle

$$360 - 300 = 60^\circ$$

$\theta$  in Quad IV,  $\theta' = 360^\circ - \theta$

$$\theta' = 2\pi - \theta$$

Theorem:

For an angle  $\theta$  in standard position

$$\sin \theta = \pm \sin \theta', \quad \cos \theta = \pm \cos \theta'$$

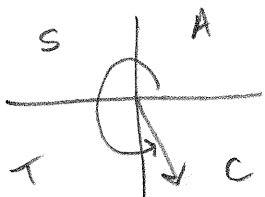
$$\tan \theta = \pm \tan \theta', \quad \sec \theta = \pm \sec \theta'$$

$$\csc \theta = \pm \csc \theta', \quad \cot \theta = \pm \cot \theta'$$

where  $\theta'$  is the reference angle and the sign is determined by the quadrant in which  $\theta$  lies.

Ex:  $\theta = 300^\circ$

$$\sin 300^\circ = -\sin 60^\circ$$

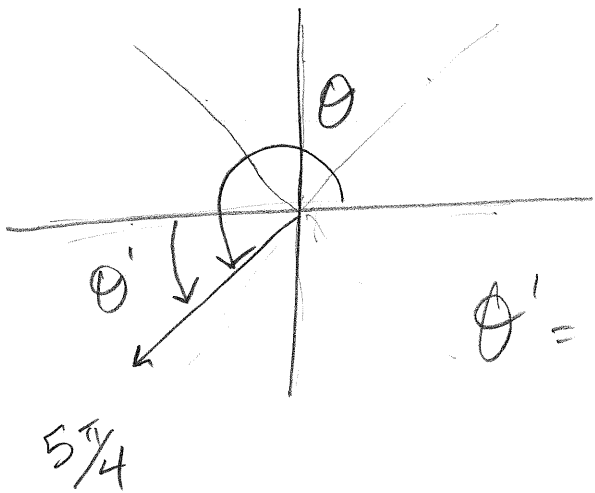


$$\begin{aligned} \theta' &= 360 - 300 \\ &= 60^\circ \end{aligned}$$

$$= -\frac{\sqrt{3}}{2}$$

$$\theta = \frac{5\pi}{4}$$

$$\tan \theta = ? \quad \cos \theta =$$



$$\theta' = \frac{\pi}{4}$$

$$\theta' = \frac{5\pi}{4} - \pi = \frac{5\pi}{4} - \frac{4\pi}{4} = \frac{\pi}{4}$$

$$\tan \frac{5\pi}{4} = + \tan \frac{\pi}{4} = 1 \quad \cos \theta = - \cos \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\tan \frac{5\pi}{4} = 1, \quad \cos \frac{5\pi}{4} = -\frac{\sqrt{2}}{2}$$

## Sec 2.1 The Unit Circle and Graphing

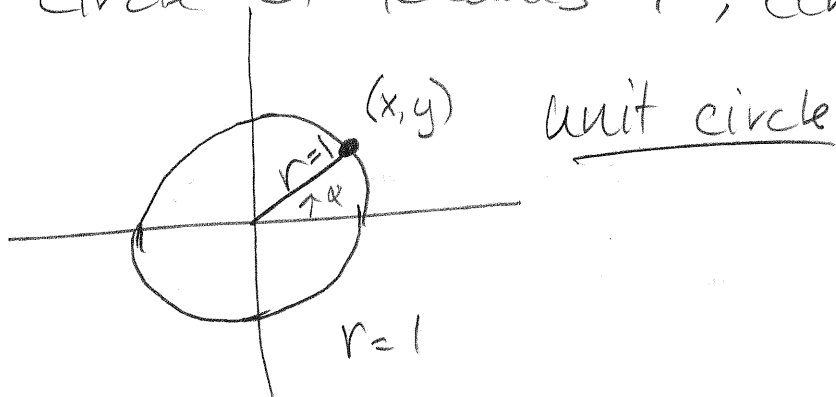
Recall:  $\alpha$  in standard position

$$\sin \alpha = \frac{y}{r}, \quad \cos \alpha = \frac{x}{r}, \quad \tan \alpha = \frac{y}{x}$$

$$\csc \alpha = \frac{r}{y}, \quad \sec \alpha = \frac{r}{x}, \quad \cot \alpha = \frac{x}{y}$$

What happens when  $r=1$

Circle of Radius 1, centered at origin



$$\sin \alpha = \frac{y}{r} = y \quad \cos \alpha = \frac{x}{r} = x \quad \tan \alpha = \frac{y}{x}$$

$$\csc \alpha = \frac{1}{y} \quad \sec \alpha = \frac{1}{x} \quad \cot \alpha = \frac{x}{y}$$

Unit circle: each coordinate is  $(\cos \alpha, \sin \alpha)$

## Graphing the Sine Function

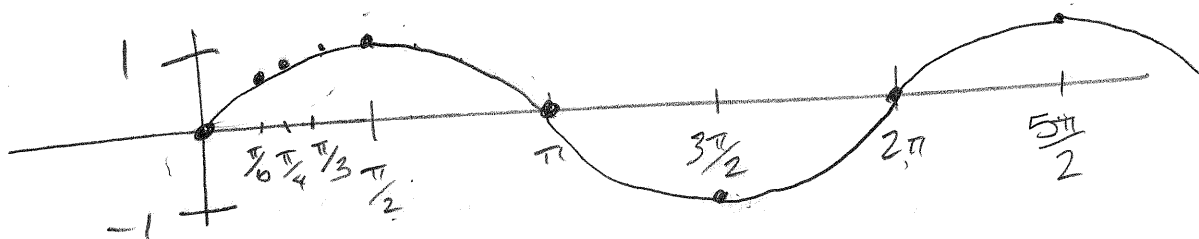
$y = \sin(x)$   
 ↑  
 output value

$y = x^2$   
 ↑  
 input value  
 (Real Numbers)  
 $x$  is in Radians

Table:

$x$	0	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$
$y = \sin x$	0	1	0	-1	0

← 5 Key Points



if we keep going it just starts  
to repeat meaning  $y = \sin x$   
is a periodic function

the smallest positive constant  $a$   
that is when the periodic function  
starts to repeat is the called  
the period

$$y = \sin x$$

$$\text{period} = 2\pi$$

Our sine curve is called

- Sine wave ← most common
- a sinusoidal wave
- a sinusoid

