

# Sec 6.4 A General Approach to Factoring

A polynomial is completely factored when both of the following are satisfied

1. It has to be written as a product of prime polynomials with integer coefficients

Ex:  $x^4 - 81$

$(x^2 + 9)(x^2 - 9)$  ← Not finished

$(x^2 + 9)(x - 3)(x + 3)$  ✓

2. None of the polynomial factors can be factored further

$2x^2 + 14x + 24$

$(2x + 6)(x + 4)$

$2(x + 3)(x + 4)$

# Factoring a Polynomial

1<sup>st</sup> Factor out any common factor

2<sup>nd</sup> What type do I have?

Binomial?

- Check if it's difference of Squares,  
difference of cubes, or a  
sum of cubes.

Trinomial?

- Check to see if it's a  
perfect square trinomial <sup>2</sup>

$$\text{Ex: } x^2 + 14x + 49 = (x+7)^2$$

$\begin{array}{ccc} \uparrow & & \uparrow \\ x^2 & 2 \cdot x \cdot 7 & 7^2 \end{array}$  ✓

- factor using <sup>x</sup> methods from 6.2

Does it have more than 3 terms?

- try factoring by grouping

$$2x^3 + 10x^2 - 4x$$

$$2x(x^2 + 5x - 2)$$

$$4t^2 + 1$$

prime

#68

$$16x^3 + 32x^2 - 9x - 18$$

$$16x^2(x+2) - 9(x+2)$$

$$(x+2)(16x^2 - 9)$$

$$(x+2)(4x+3)(4x-3)$$